

Exact solution of the random close packing problem in d=2 and entropy-stability competition



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Abstract: Predicting the densest random packing fraction of mono-disperse discs is relevant to a range of disciplines and technologies. Until recently, it was a decades-long unsolved problem. The difficulties were that it was ill-defined in the absence of a disorder criterion and that the packing fraction depends on the packing protocol. Since protocols depend on a large number of continuous parameters, it was difficult to find a general theoretical solution that applies to this infinite-parameter space.

I present here a recent new approach that has opened the door to an exact solution in two dimensions. I first formulate the problem in a well-posed form for planar packings of discs. Next, I show that all the infinitely possible packing protocols can be parametrised by the distribution of the cell order. I then describe a systematic criterion that ensures disorder. Then,

I derive the exact value for the random close packing fraction: φ RCP = 0.852514....

The advantages of this method are that it:

- (i) yields directly the packing fraction;
- (ii) parametrises all possible packing protocols;
- (iii) makes it possible to define and limit all types of disorder;
- (iv) it can be used to predict the highest packing fraction for families of protocols.
- Finally, I will discuss the role of entropy and entropy-stability competition in this problem and in quasi-static dynamics of granular matter in general.



Biography of speaker: Raphael Blumenfeld received PhD in Theoretical Physics from Tel Aviv University and since then held positions at: the Cavendish Laboratory, University of Cambridge; Princeton University; Los Alamos National Laboratory, USA; then at Princeton University again. He returned to the Cavendish Laboratory Cambridge in 1998 and held a simultaneous position at Imperial College London. Since 2009 he is a Bye-Fellow and College Lecturer at Gonville & Caius College, University of Cambridge. Currently, he is the Director of Studies for the Physics Natural Science at the college. He is also a Distinguished Visiting Professor at a university in China, a High Level Foreign Talent, and a 1000-Talent plan award recipient from the Chinese government. He has over 130 publications, over a 100 of which in peer-reviewed journals. Raphael Blumenfeld 's research interests have focused in recent years on the physics of a-thermal systems and, in particular, on the behaviour granular, cellular and porous materials. These type of systems are relevant in many contexts and a wide range of scales; from powders and suspensions of micronsize particles to the structure of the cosmic web on the scale of the universe. His research progresses in several directions. One is the construction of a statistical mechanics formalism for these non-ergodic and far-from-equilibrium systems. Another is the formulation of a fundamental stress theory for granular materials. A third direction is construction of a physicsbased model for the dynamic behaviour of particulate systems.

